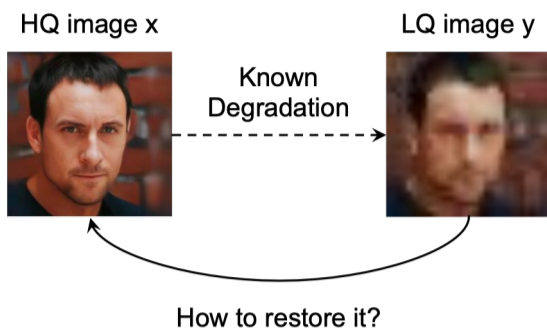




## Introduction

### [Task Definition]



Given a known degradation operator  $H$  and the low-quality image  $y$ , inverse problems aims to restore the high-quality image  $x$  from  $y = Hx + n$ . Corresponding image restoration tasks including SR, colorization, deblurring, inpainting, ...

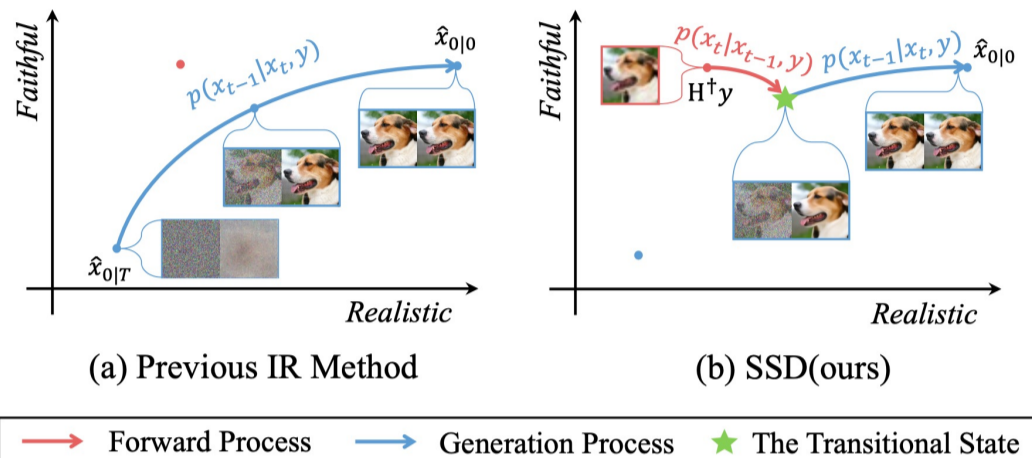
**This work mainly focus on Zero-Shot IR with pretrained DM.**

**What Previous Works Do:** Modify the posterior sampling process, from  $p(x|z)$  to  $p(x|z, y)$ , treat it as a conditional generation task (DDRM, DPS, DDNM), which requires more steps to restore.

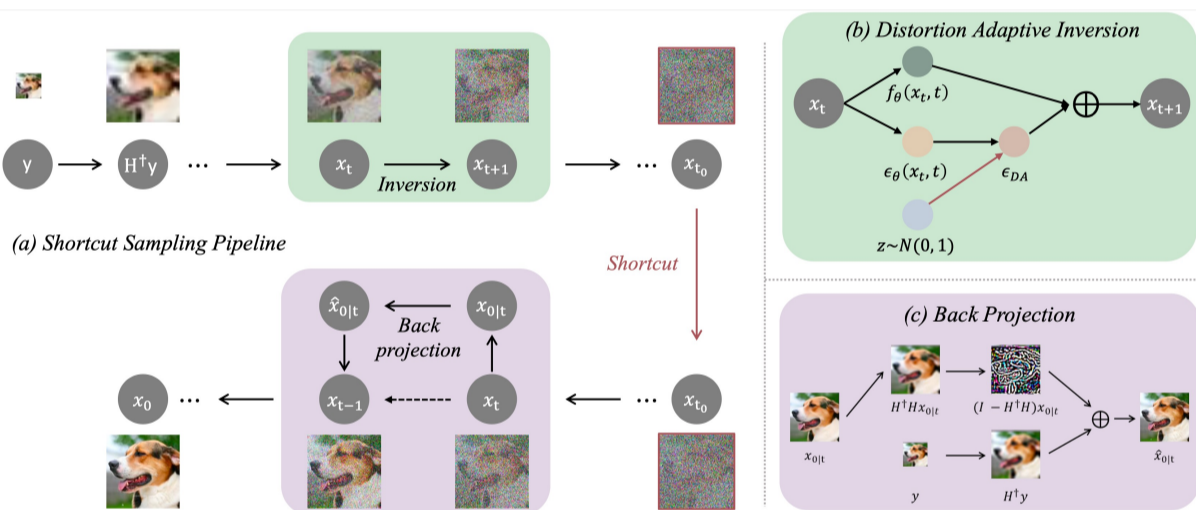
**What We Do:** Not all the sampling steps are required. The early stage of denoising can be replaced by a specific “inversion process”

**What We Achieve:**

- An inversion process that preserve the layout and structure of LQ images;
- A novel method that achieve SOTA performance with fewer steps;



## Method



### a). Shortcut Sampling Pipeline

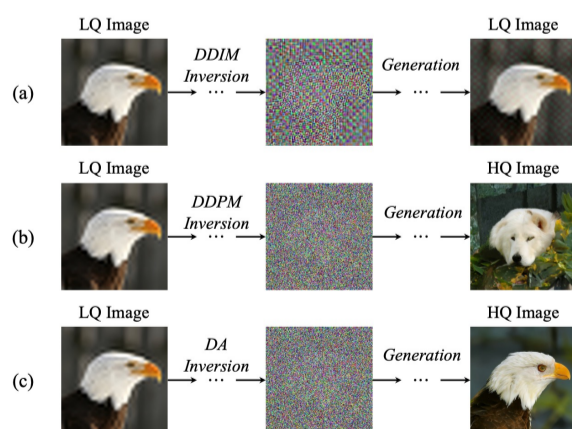
We propose Shortcut Sampling for Diffusion(SSD). Different from previous methods that initiate from noise, We introduce Distortion Adaptive Inversion to replace the early stage of denoising, along with back projection during denoising to force consistency.

### b). Distortion Adaptive Inversion

**Criteria (i):** Contain information from the input image;

**Criteria (ii):** Retain the capacity for generating HQ images;

DDIM Inversion cannot satisfy Criteria (ii), due to the predict noise deviates from  $\mathcal{N}(0, I)$



We propose distortion adaptive inversion to satisfy both:

$$x_{t+1} = \sqrt{\alpha_{t+1}}f_{\theta}(x_t, t) + \sqrt{1 - \alpha_{t+1} - \eta\beta_{t+1}}\epsilon_{\theta}(x_t, t) + \sqrt{\eta\beta_{t+1}}z, \quad z \sim \mathcal{N}(0, I)$$

### c). Back Projection

Denosing Step: 
$$x_{0|t} = \frac{x_t - \sqrt{1 - \alpha_t}\epsilon_{\theta}(x_t, t)}{\sqrt{\alpha_t}}$$

Back Projection Step: 
$$x_{t-1} = (I - H^T H)x_{0|t} + H^T y$$

## Results

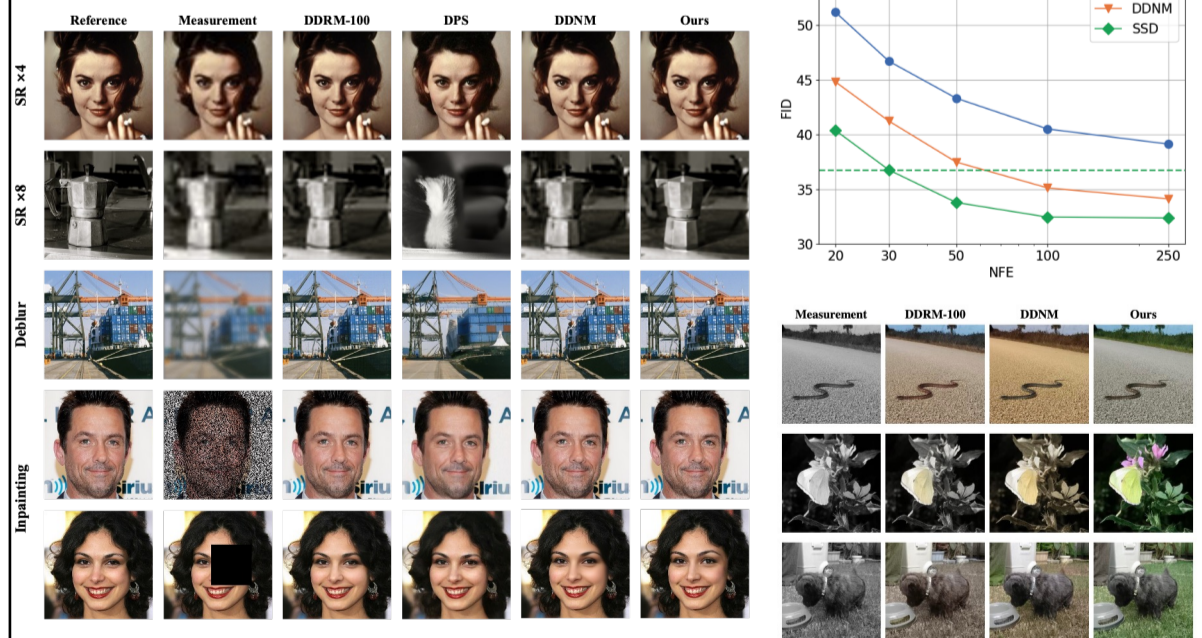
### Quantitative Evaluation

| CelebA Method         | SR × 4                              |                                     |                             | SR × 8                                    |                       |                       | Colorization          |                       |                       | Deblur (gauss) |  |  | NFEs↓ |
|-----------------------|-------------------------------------|-------------------------------------|-----------------------------|---|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|----------------|--|--|-------|
|                       | PSNR↑ / FID↓ / LPIPS↓               | PSNR↑ / FID↓ / LPIPS↓               | PSNR↑ / FID↓ / LPIPS↓       | FID↓ / LPIPS↓                             | PSNR↑ / FID↓ / LPIPS↓ | PSNR↑ / FID↓ / LPIPS↓ | PSNR↑ / FID↓ / LPIPS↓ | PSNR↑ / FID↓ / LPIPS↓ | PSNR↑ / FID↓ / LPIPS↓ |                |  |  |       |
| $H^T y$               | 28.02 / 128.22 / 0.301              | 24.77 / 153.86 / 0.460              | 43.99 / 0.197               | 19.96 / 116.28 / 0.564                    | 0                     |                       |                       |                       |                       |                |  |  |       |
| DDRM-100              | 28.84 / 40.52 / 0.214               | 26.47 / 45.22 / 0.273               | 25.88 / 0.156               | 36.17 / 15.32 / 0.119                     | 100                   |                       |                       |                       |                       |                |  |  |       |
| DPS                   | 24.71 / 34.69 / 0.304               | 22.38 / 41.01 / 0.348               | N/A                         | 24.89 / 32.64 / 0.288                     | 250                   |                       |                       |                       |                       |                |  |  |       |
| DDNM-100              | 28.85 / 35.13 / 0.206               | 26.53 / 44.22 / 0.272               | 23.65 / 0.138               | 38.70 / 4.48 / 0.062                      | 100                   |                       |                       |                       |                       |                |  |  |       |
| <b>SSD-100 (ours)</b> | 28.84 / <b>32.41</b> / <b>0.202</b> | 26.44 / 42.42 / <b>0.267</b>        | <b>23.62</b> / <b>0.138</b> | 38.62 / <b>4.36</b> / <b>0.060</b>        | 100                   |                       |                       |                       |                       |                |  |  |       |
| DDRM-30               | 28.62 / 46.72 / 0.221               | 26.28 / 49.32 / 0.281               | 27.69 / 0.214               | 36.05 / 15.71 / 0.122                     | 30                    |                       |                       |                       |                       |                |  |  |       |
| DDNM-30               | <b>28.76</b> / 41.36 / 0.213        | <b>26.41</b> / 48.25 / 0.277        | 25.25 / 0.184               | 37.40 / 6.65 / 0.084                      | 30                    |                       |                       |                       |                       |                |  |  |       |
| <b>SSD-30 (ours)</b>  | 28.71 / <b>36.77</b> / <b>0.208</b> | 26.32 / <b>44.97</b> / <b>0.271</b> | <b>24.11</b> / <b>0.159</b> | <b>38.34</b> / <b>4.98</b> / <b>0.065</b> | 30                    |                       |                       |                       |                       |                |  |  |       |

| ImageNet Method       | SR × 4                                     |                                     |                             | SR × 8                                    |                       |                       | Colorization          |                       |                       | Deblur (gauss) |  |  | NFEs↓ |
|-----------------------|--|-------------------------------------|-----------------------------|---|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|----------------|--|--|-------|
|                       | PSNR↑ / FID↓ / LPIPS↓                      | PSNR↑ / FID↓ / LPIPS↓               | PSNR↑ / FID↓ / LPIPS↓       | FID↓ / LPIPS↓                             | PSNR↑ / FID↓ / LPIPS↓ | PSNR↑ / FID↓ / LPIPS↓ | PSNR↑ / FID↓ / LPIPS↓ | PSNR↑ / FID↓ / LPIPS↓ | PSNR↑ / FID↓ / LPIPS↓ |                |  |  |       |
| $H^T y$               | 26.26 / 106.01 / 0.322                     | 22.86 / 124.89 / 0.4690             | 27.40 / 0.231               | 19.33 / 102.33 / 0.553                    | 0                     |                       |                       |                       |                       |                |  |  |       |
| DDRM-100              | 27.40 / 43.27 / 0.260                      | 23.74 / 83.08 / 0.420               | 36.44 / 0.224               | 36.48 / 11.81 / 0.121                     | 100                   |                       |                       |                       |                       |                |  |  |       |
| DPS                   | 20.34 / 72.33 / 0.485                      | 18.38 / <b>76.89</b> / 0.538        | N/A                         | 24.89 / 32.64 / 0.288                     | 250                   |                       |                       |                       |                       |                |  |  |       |
| DDNM-100              | 27.44 / 39.42 / 0.251                      | <b>23.80</b> / 80.09 / 0.412        | 36.46 / 0.219               | <b>40.48</b> / 3.33 / 0.041               | 100                   |                       |                       |                       |                       |                |  |  |       |
| <b>SSD-100 (ours)</b> | <b>27.45</b> / <b>37.69</b> / <b>0.248</b> | 23.76 / 82.11 / <b>0.409</b>        | <b>35.40</b> / <b>0.215</b> | 40.32 / <b>3.07</b> / <b>0.039</b>        | 100                   |                       |                       |                       |                       |                |  |  |       |
| DDRM-30               | 27.17 / 46.14 / 0.269                      | 23.50 / 84.53 / 0.426               | 36.48 / 0.237               | 35.90 / 13.35 / 0.130                     | 30                    |                       |                       |                       |                       |                |  |  |       |
| DDNM-30               | <b>27.22</b> / 40.12 / 0.256               | <b>23.53</b> / <b>74.60</b> / 0.414 | 36.46 / 0.229               | 37.67 / 6.91 / 0.081                      | 30                    |                       |                       |                       |                       |                |  |  |       |
| <b>SSD-30 (ours)</b>  | 27.13 / <b>38.24</b> / <b>0.251</b>        | 23.44 / 76.35 / <b>0.411</b>        | <b>36.22</b> / <b>0.223</b> | <b>39.23</b> / <b>4.64</b> / <b>0.053</b> | 30                    |                       |                       |                       |                       |                |  |  |       |

### Noiseless Image Restoration



### Noisy Image Restoration

We restrict the utilization of back projection to the middle stage to adapt to noisy tasks

